

1. The Well-Ordering Principle (WOP) states that every nonempty subset of \mathbb{Z}^+ contains _____.

(3 points)

- A. a largest element
- ✓ B. a smallest element
- C. a total order
- D. a dual subset

2. The induction step for the Principle of Mathematical Induction (PMI) insures which of the following logical implications (denoted by \rightarrow) for an arbitrary integer k in Z^+ ?

(3 points)

- A. $p(k+1) \rightarrow p(k)$
- B. $p(k) \rightarrow p(1)$
- ✓ C. $p(k) \rightarrow p(k+1)$
- D. $p(k-1) \rightarrow p(k)$

3. Which one of the following set relations is valid for the recursively defined sets A and B below?

$$\{1 \in A, \forall y \in A, y + 1 \in A\}$$

$$\{2 \in B, \forall z \in B, z \times 2 \in B\}$$

(3 points)

1. A is a proper subset of B.
- ✓ 2. B is a proper subset of A.
3. The symmetric difference between A and B is the empty set.
4. None of the above.