An undirected graph is defined as follows:

 $\begin{array}{l} V = \{ \; i \mid 0 <= i < 10 \; \} \\ E = \{ \; (0,1), \; (0,3), \; (1,9), \; (3,5), \; (3,7), \; (4,6), \; (5,9), \; (6,8) \; \} \end{array}$ 

Question 1: How many connected components are in the graph?

**Question 2:** Which nodes are in the one cycle in this graph (just list the node numbers with spaces between them).

**Question 3:** Is this graph bipartite?

Question 4: Which of the following is an adjacency matrix for the graph?

Α	В	C
0 1 2 3 4 5 6 7 8 9	0 1 2 3 4 5 6 7 8 9	0 1 2 3 4 5 6 7 8 9
0   0 1 0 1 0 0 0 0 0 0	0   1 1 0 1 0 0 0 0 0	0 0 1 0 1 0 0 0 0 0 0
1 0 0 0 0 0 0 0 0 1	1   1 1 0 0 0 0 0 0 1	1 1 0 0 0 0 0 0 0 1
2 0 0 0 0 0 0 0 0 0 0	2 0 0 1 0 0 0 0 0 0	2 0 0 0 0 0 0 0 0 0 0 0
3   0 0 0 0 0 1 0 1 0 0	3   1 0 0 1 0 1 0 1 0 0	3   1 0 0 0 0 1 0 1 0 0
4   0 0 0 0 0 0 1 0 0 0	4   0 0 0 0 1 0 1 0 0 0	4   0 0 0 0 0 0 1 0 0 0
5   0 0 0 0 0 0 0 0 0 1	5   0 0 0 1 0 1 0 0 0 1	5 0 0 0 1 0 0 0 0 1
6   0 0 0 0 0 0 0 0 1 0	6   0 0 0 0 1 0 1 0 1 0	6 0 0 0 0 1 0 0 0 1 0
7   0 0 0 0 0 0 0 0 0 0 0	7   0 0 0 1 0 0 0 1 0 0	7 0 0 0 1 0 0 0 0 0
8   0 0 0 0 0 0 0 0 0 0	8   0 0 0 0 0 0 1 0 1 0	8 0 0 0 0 0 0 1 0 0 0
9   0 0 0 0 0 0 0 0 0 0	9   0 0 0 0 0 1 0 0 0 1	9   0 1 0 0 0 1 0 0 0 0

## **General Graph Clicker Questions**

An undirected graph is defined as follows:

 $V = \{ i \mid 0 \le i < 10 \}$  $E = \{ (0,1), (0,3), (1,9), (3,5), (3,7), (4,6), (5,9), (6,8) \}$ 

Question 1. How many connected components are in the graph?

Answer: The easiest way to answer this is to draw the graph:



The answer is three.

Question 2. Which nodes are in the one cycle in this graph?

Answer: Look at the graph above: 0, 1, 3, 5, 9 (not in that order)

Question 3. Is this graph bipartite?

No -- it has an odd cycle, and if you think about it, an odd cycle cannot be in a bitpartite graph.

Question 4. Which of the following is an adjacency matrix of the graph?

You can use process of elimination - Matrix A doesn't have (1,0), (3,0), etc. Since the graph is undirected, you need to have entries (i,j) and (j,i). That rules out matrix A.

Matrix B has self-edges: (0,0), (1,1), etc, which the given graph doesn't have.

Matrix C is good.