

For each of the following procedures, enter the big-O of its running times. Please represent v 's size as m , and express your big-O as a function of n and m .

Question 1:

```
#include <vector>
using namespace std;

void a(vector <int> &v, int n)
{
    int i;
    for (i = 0; i < n; i++) {
        v.push_back(i*i);
    }
}
```

Question 2:

```
#include <vector>
#include "nlohmann/json.hpp"
using namespace std;
using nlohmann::json;

string vtojs(vector <string> &v)
{
    json j;
    size_t i;

    for (i = 0; i < v.size(); i++) j[v[i]] = i;
    return j.dump(2);
}
```

Please assume that all of the strings in v are less than 10 characters.

Question 3:

```
#include <vector>
#include <set>
#include <iostream>
using namespace std;

bool b(vector <int> &v, int n)
{
    multiset <int> s;
    int i;

    for (i = 0; i < v.size(); i++) {
        s.insert(v[i]);
    }
    return (s.find(n) != s.end());
}
```

Question 4:

```
#include <vector>
#include <iostream>
using namespace std;

int find(vector <int> &v, int n)
{
    int l, h, m;

    l = 0;
    h = v.size();

    while (l < h) {
        m = (l+h)/2;
        if (m == h) m--;
        if (v[m] == n) return m;
        if (v[m] > n) {
            h = m;
        } else {
            l = m+1;
        }
    }
    return l;
}
```

Clicker Question Answers

- Question 1: `push_back()` is $O(1)$ and the loop iterates n times: $O(n)$.
- Question 2: Recall, JSON objects are implemented with maps. This is why they are sorted when you print or `dump()` them. Therefore, this is $O(m \log m)$.
- Question 3: The loop iterates m times, and the `insert()` operation on average is $O(\log m)$. The last `find()` is $O(\log m)$, so it may be ignored. The answer is $O(m \log m)$.
- Question 4: The variable m is set to the midpoint between l and h . Thus, $(h-l)$ is reduced by half at each iteration. $(h-l)$ starts at m , so this loop iterates $O(\log m)$ times. The answer is $O(\log m)$.