Question 1: What is the output of the following program?

```
#include <iostream>
using namespace std;
int s(int n)
{
    if (n == 0) return 0;
    return n + s(n-1);
}
int main()
{
    cout << s(10) << endl;
}</pre>
```

Question 2: What is the running time of *s*(*n*)?

(In these questions, use the carat symbol (^) for exponentiation). **Question 3**: What is the output of the following program?

```
#include <iostream>
using namespace std;
string t(string v)
{
   string tmp;
   if (v.size() == 0) return "";
   tmp.push_back(v[0]);
   return t(v.substr(1)) + tmp;
}
int main()
{
   cout << t("Fred") << endl;
}</pre>
```

Question 4: What is the running time of t(v), where n = v.size()?

Question 5: What would be the running time of t(v) if v were a reference parameter?

Question 1

- s(10) returns 10 + s(9).
- s(9) returns 9 + s(8).
- s(8) returns 8 + s(7).
- And so on
- s(0) returns 0

So, $\mathbf{s}(\mathbf{n})$ returns n + (n-1) + ... + 2 + 1, which is n(n+1)/2. The answer is 55.

Question 2

Answer: It makes *n* recursive calls, and each call does O(1) work (besides the recursion). So the answer is O(n).

Question 3

- s("Fred") sets **tmp** to "F" and calls s("red"). It returns s("red") + "F".
- s("red") sets **tmp** to "r" and calls s("ed"). It returns s("ed") + "r".
- s("ed") sets **tmp** to "e" and calls s("d"). It returns s("d") + "e".
- s("d") sets **tmp** to "d" and calls s(""). It returns s("") + "d".
- s("") returns "".
- So, s("d") returns "d".
- So, s("ed") returns "de".
- So, s("red") returns "der".
- So, s("Fred") returns "derF".

In other words it reverses the string: "derF".

Question 4

Answer: It makes *n* recursive calls; However each recursive call creates a substring of size (n-1) and then copies it when calling s() on the substring. So the running time of this is n + (n-1) + (n-2) + ... + 2 + 1, which is $O(n^2)$.

Question 5

With the reference parameter, a copy of the substring is no longer made. However, making the substring still takes O(n) work, so the running time is still O(n + (n-1) + (n-2) + ... + 2 + 1), which is still $O(n^2)$.