

For these questions, each answer is four numbers. Simply enter them on Turning point separated by spaces or commas.

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I'll also put the mathematical definition of open addressing here. From the lecture notes:

With open addressing, you test the keys in order,  $h_0, h_1, h_2, \dots$ , until you find what you're looking for or you find an empty space in the hash table.  $h_i$  is defined as follows:

$$h_i = H(\text{key}) + F(i, \text{key}), \text{ modulo the table size.}$$

$H()$  is the hash function, and  $F()$  is a function that defines how to resolve collisions. It is usually convenient to make sure that  $F(0, \text{key})$  equals zero, and it is necessary for  $F(i, \text{key})$  not to equal zero when  $i$  doesn't equal zero.

- With linear probing,  $F(i, \text{key}) = i$ .
- With quadratic probing,  $F(i, \text{key}) = i^2$ .
- With double hashing,  $F(i, \text{key}) = H_2(\text{key}) * i$ .

**Question 1:** Suppose you are looking up a value in a hash table that has 100 elements, and the hash table is pretty full. The hash function for the value returns 847298. You are using linear probing – what are the first four indices that you will test when you look up the value?

**Question 2:** Now, suppose you are using quadratic probing. What are the first four indices that you will test?

**Question 3:** Now, suppose you are using double-hashing, and the second hash function returns 92821. What are the first four indices that you will test?

## Answers

This one came from the spring 2014 midterm. Here are the answers:

**Question 1:** You start at 98, and look at successively higher indices mod 100: 98, 99, 0, 1.

**Question 2:** Now, you start at 98, and add  $0^2$ ,  $1^2$ ,  $2^2$  and  $3^2$ : 98, 99, 2, 7.

**Question 3:** Now, you start at 98, and add  $0*21$ ,  $1*21$ ,  $2*21$  and  $3*21$ : 98, 19, 40, 61.

## Grading

1 point per answer, with the following caveats:

- **Question 1:** To receive full credit on the 2nd, 3rd and 4th probes, they had to equal the previous probe plus one, mod 100.
- **Question 1:** If you said 1 instead of 0, you got half credit.
- **Question 1:** If you forgot the mod 100 when you added one, you got half credit.
- **Question 2:** To get full credit, your answer for the first probe had to equal the answer for the first probe in Question 1.
- **Question 2:** The other probes needed to be relative to the first probe.
- **Question 2:** If you forgot the mod 100, you got half credit.
- **Question 2:** On the third and fourth probes, if you were off by one, you got half credit.
- **Question 3:** To get full credit, your answer for the first probe had to equal the answer for the first probe in Question 1.
- **Question 3:** The other probes needed to be relative to the first probe.
- **Question 3:** If you forgot the mod 100, you got half credit.
- **Question 3:** On the second, third and fourth probes, if you were off by one, you got half credit.